

ภาคผนวก ง

- วิเคราะห์ความแปรปรวน

วิเคราะห์ความแปรปรวน

	ก่อนการทดลอง	หลังการทดลอง	ติดตามผล	Subject Total
กลุ่มทดลอง	7.77	12.08	10.36	30.21
	11.48	11.32	10.60	33.40
	9.64	11.43	11.59	32.66
	8.31	14.80	12.75	35.86
	10.68	16.34	16.14	43.16
	10.89	12.17	13.89	36.95
	9.98	9.95	11.74	31.67
	11.11	12.51	12.51	36.13
Total	79.86	100.60	99.58	280.04
กลุ่มควบคุม	9.62	9.09	12.20	30.91
	9.53	10.23	10.23	29.99
	10.17	9.90	10.22	30.29
	8.35	8.14	9.38	25.87
	9.39	10.58	8.63	28.60
	8.75	9.70	8.93	27.38
	9.42	7.48	7.95	24.85
	10.53	7.14	9.58	27.25
Total	75.76	72.26	77.12	225.14
Interval Total	155.62	172.86	176.70	505.18

การหาผลรวมกำลังสอง (Sum of Squares)

$$\begin{aligned}
 1. \ SS_{\text{total}} &= \sum X^2 - \frac{(\sum X)^2}{N} \\
 &= 7.77^2 + 11.48^2 + 9.64^2 + \dots + 8.93^2 + 7.95^2 + 9.58^2 - \frac{(505.18)^2}{48} \\
 &= 5,509.02 - 5316.81 \\
 &= 192.21
 \end{aligned}$$

$$\begin{aligned}
 2. \ SS_{\text{subj}} &= \frac{\sum T_s^2}{i} - \frac{(\sum X)^2}{N} \\
 &= \frac{30.21^2 + 33.40^2 + 32.66^2 + \dots + 27.38^2 + 24.85^2 + 27.25^2}{3} - \frac{(505.18)^2}{48} \\
 &= 5428.85 - 5316.81 \\
 &= 112.04
 \end{aligned}$$

$$\begin{aligned}
 3. \ SS_{\text{groups}} &= \frac{(\sum T_g^2)}{ni} - \frac{(\sum X)^2}{N} \\
 &= \frac{280.04^2 + 225.14^2}{(8)(3)} - \frac{(505.18)^2}{48} \\
 &= 5379.60 - 5316.81 \\
 &= 62.79
 \end{aligned}$$

$$\begin{aligned}
 4. \ SS_{\text{intervals}} &= \frac{(\sum T_i^2)}{ng} - \frac{(\sum X)^2}{N} \\
 &= \frac{155.62^2 + 172.86^2 + 176.7^2}{(8)(2)} - \frac{(505.18)^2}{48} \\
 &= 5332.57 - 5316.81 \\
 &= 15.76
 \end{aligned}$$

$$\begin{aligned}
 5. \quad SS_{\text{cells}} &= \frac{(\sum T^2_{ij})}{n} - \frac{(\sum X)^2}{N} \\
 &= \frac{79.86^2 + 100.60^2 + 99.58^2 + 75.76^2 + 72.26^2 + 77.12^2}{8} - \frac{(505.18)^2}{48} \\
 &= 5415.34 - 5316.81 \\
 &= 98.53
 \end{aligned}$$

$$\begin{aligned}
 6. \quad SS_{I \times G} &= SS_{\text{cells}} - SS_{\text{groups}} - SS_{\text{intervals}} \\
 &= 98.53 - 62.79 - 15.76 \\
 &= 19.98
 \end{aligned}$$

$$\begin{aligned}
 7. \quad SS_{\text{w/in subj}} &= SS_{\text{total}} - SS_{\text{between subj}} \\
 &= 192.21 - 112.04 \\
 &= 80.17
 \end{aligned}$$

$$\begin{aligned}
 8. \quad SS_{\text{Ss w/in groups}} &= SS_{\text{between subj}} - SS_{\text{groups}} \\
 &= 112.04 - 62.79 \\
 &= 49.25
 \end{aligned}$$

$$\begin{aligned}
 9. \quad SS_{I \times \text{Ss w/in groups}} &= SS_{\text{w/in subj}} - SS_{\text{intervals}} - SS_{I \times G} \\
 &= 80.17 - 15.76 - 19.98 \\
 &= 44.43
 \end{aligned}$$

การแจก Degree of freedom

$$\begin{aligned}
 1. \ df_{w/in \text{ Subj}} &= df_{total} - df_{between \text{ subj}} \\
 &= 47 - 15 \\
 &= 32
 \end{aligned}$$

$$\begin{aligned}
 2. \ df_{Ss \text{ w/in groups}} &= df_{between \text{ subj}} - df_{groups} \\
 &= 15 - 1 \\
 &= 14
 \end{aligned}$$

$$\begin{aligned}
 3. \ df_{I \times Ss \text{ w/in groups}} &= df_{w/in \text{ subj}} - df_{intervals} - df_{I \times G} \\
 &= 32 - 2 - 2 \\
 &= 28
 \end{aligned}$$

$$\begin{aligned}
 4. \ df_{between \text{ subj}} &= df_{total} - df_{w/in \text{ Subj}} \\
 &= 47 - 32 \\
 &= 15
 \end{aligned}$$

$$\begin{aligned}
 5. \ df_{groups} &= g - 1 \\
 &= 2 - 1 \\
 &= 1
 \end{aligned}$$

$$\begin{aligned}
 6. \ df_{intervals} &= i - 1 \\
 &= 3 - 1 \\
 &= 2
 \end{aligned}$$

$$\begin{aligned}
 7. \ df_{I \times G} &= (I - 1) \times (G - 1) \\
 &= (3 - 1) \times (2 - 1) \\
 &= 2
 \end{aligned}$$

คำนวณหาค่า MS

$$1. \ MS_{\text{groups}} = \frac{SS_{\text{groups}}}{df_{\text{groups}}}$$

$$\begin{aligned}
 &= \frac{62.79}{1} \\
 &= 62.79
 \end{aligned}$$

$$2. \ MS_{\text{Ss w/in groups}} = \frac{SS_{\text{Ssw/in groups}}}{df_{\text{Ssw/in groups}}}$$

$$\begin{aligned}
 &= \frac{49.25}{14} \\
 &= 3.52
 \end{aligned}$$

$$3. \ MS_{\text{intervals}} = \frac{SS_{\text{intervals}}}{df_{\text{intervals}}}$$

$$\begin{aligned}
 &= \frac{15.76}{2} \\
 &= 7.88
 \end{aligned}$$

$$\begin{aligned}
 4. \quad MS_{I \times G} &= \frac{SS_{I \times G}}{df_{I \times G}} \\
 &= \frac{19.98}{2} \\
 &= 9.99 \approx 10.00
 \end{aligned}$$

$$\begin{aligned}
 5. \quad MS_{I \times Ss \text{ w/in groups}} &= \frac{SS_{I \times Ss \text{ w/in groups}}}{df_{I \times Ss \text{ w/in groups}}} \\
 &= \frac{44.43}{28} \\
 &= 1.59
 \end{aligned}$$

การทดสอบผลหลักและปฏิสัมพันธ์ระหว่างตัวแปรต้น

(Main and interactions two factors)

1. ผลหลักของตัวแปรระหว่างตัวอย่าง

“วิธีการปรึกษากลุ่มตามแนวทฤษฎีทางเลือก” (G)

$$\begin{aligned}
 F_{\text{groups}} &= \frac{MS_{\text{groups}}}{MS_{Ss \text{ w/in groups}}} \\
 &= \frac{62.79}{3.52} \\
 &= 17.84
 \end{aligned}$$

2. ผลหลักของตัวแปรภายในตัวอย่าง “ระยะเวลา” (I)

$$\begin{aligned}
 F_{\text{intervals}} &= \frac{MS_{\text{intervals}}}{MS_{\text{I} \times \text{Ss w/in groups}}} \\
 &= \frac{7.88}{1.59} \\
 &= 4.96
 \end{aligned}$$

3. ปฏิสัมพันธ์ระหว่างระยะเวลาและวิธีการทดลอง (I X G)

$$\begin{aligned}
 F_{\text{I} \times \text{G}} &= \frac{MS_{\text{I} \times \text{G}}}{MS_{\text{I} \times \text{Ss w/in groups}}} \\
 &= \frac{10}{1.59} \\
 &= 6.29
 \end{aligned}$$

การทดสอบผลย่อย (Simple Effect)

ผลย่อยของตัวแปรวัดซ้ำ

1. ผลย่อยของระยะเวลาในกลุ่มทดลอง

(Simple effects of interval at method = experiment)

$$\begin{aligned}
 1.1 \ SS_{\text{total}} &= \sum X^2 - \frac{(\sum X)^2}{N} \\
 &= 7.77^2 + 11.48^2 + 9.64^2 + \dots + 13.89^2 + 11.74^2 + 12.51^2 - \\
 &\quad \frac{(280.04)^2}{24} \\
 &= 3368.53 - 3267.60 \\
 &= 100.93
 \end{aligned}$$

$$\begin{aligned}
 1.2 \ SS_{\text{Subj}} &= \frac{\sum T_s^2}{q} - \frac{(\sum X)^2}{N} \\
 &= \frac{30.21^2 + 33.40^2 + 32.66^2 + \dots + 36.95^2 + 31.67^2 + 36.13^2}{3} - \frac{(280.04)^2}{24} \\
 &= 3305.76 - 3267.60 \\
 &= 38.16
 \end{aligned}$$

$$\begin{aligned}
 1.3 \ SS_{\text{intervals}} &= \frac{\sum T_w^2}{n} - \frac{(\sum X)^2}{N} \\
 &= \frac{79.86^2 + 100.6^2 + 99.58^2}{8} - \frac{(280.04)^2}{24} \\
 &= 3301.77 - 3267.60 \\
 &= 634.17
 \end{aligned}$$

$$\begin{aligned}
 1.4 \ SS_{\text{error}} &= SS_{\text{total}} - SS_{\text{subj}} - SS_{\text{intervals}} \\
 &= 100.93 - 38.16 - 34.17 \\
 &= 28.6
 \end{aligned}$$

$$\begin{aligned}
 1.5 \ df_{\text{between subj}} &= n - 1 \\
 &= 8 - 1 \\
 &= 7
 \end{aligned}$$

$$\begin{aligned}
 1.6 \ df_{\text{intervals}} &= q - 1 \\
 &= 3 - 1 \\
 &= 2
 \end{aligned}$$

$$\begin{aligned}
 1.7 \quad df_{\text{error}} &= (q - 1) \times (n - 1) \\
 &= (3 - 1) \times (8 - 1) \\
 &= 14
 \end{aligned}$$

$$\begin{aligned}
 1.8 \quad df_{\text{total}} &= df_{\text{between subj}} + df_{\text{intervals}} + df_{\text{error}} \\
 &= 7 + 2 + 14 \\
 &= 23
 \end{aligned}$$

$$\begin{aligned}
 1.9 \quad MS_{\text{intervals}} &= \frac{SS_{\text{intervals}}}{df_{\text{intervals}}} \\
 &= \frac{34.17}{2} \\
 &= 17.09
 \end{aligned}$$

$$\begin{aligned}
 1.10 \quad MS_{\text{error}} &= \frac{SS_{\text{error}}}{df_{\text{error}}} \\
 &= \frac{28.6}{14} \\
 &= 2.04
 \end{aligned}$$

$$\begin{aligned}
 1.11 \quad F &= \frac{MS_{\text{intervals}}}{MS_{\text{error}}} \\
 &= \frac{17.09}{2.04} \\
 &= 8.38
 \end{aligned}$$

2. ผลย่อยของระยะเวลาในกลุ่มควบคุม

(Simple effects of interval at method = control)

$$\begin{aligned}
 2.1 \ SS_{\text{total}} &= \sum X^2 - \frac{(\sum X)^2}{N} \\
 &= 9.62^2 + 9.53^2 + 10.17^2 + \dots + 8.93^2 + 7.95^2 + 9.58^2 - \frac{(225.14)^2}{24} \\
 &= 2140.49 - 2112.00 \\
 &= 28.49
 \end{aligned}$$

$$\begin{aligned}
 2.2 \ SS_{\text{subj}} &= \frac{\sum T_s^2}{w} - \frac{(\sum X)^2}{N} \\
 &= \frac{30.91^2 + 29.99^2 + 30.29^2 + \dots + 27.38^2 + 24.85^2 + 27.25^2}{3} - \frac{(225.14)^2}{24} \\
 &= 2123.09 - 2112.00 \\
 &= 11.09
 \end{aligned}$$

$$\begin{aligned}
 2.3 \ SS_{\text{intervals}} &= \frac{\sum T_w^2}{n} - \frac{(\sum X)^2}{N} \\
 &= \frac{75.76^2 + 72.26^2 + 77.12^2}{8} - \frac{(225.14)^2}{24} \\
 &= 2113.57 - 2112.00 \\
 &= 1.57
 \end{aligned}$$

$$\begin{aligned}
 2.4 \ SS_{\text{error}} &= SS_{\text{total}} - SS_{\text{subj}} - SS_{\text{intervals}} \\
 &= 28.49 - 11.09 - 1.57 \\
 &= 15.83
 \end{aligned}$$

$$\begin{aligned}
 2.5 \quad df_{\text{between subj}} &= n - 1 \\
 &= 8 - 1 \\
 &= 7
 \end{aligned}$$

$$\begin{aligned}
 2.6 \quad df_{\text{intervals}} &= q - 1 \\
 &= 3 - 1 \\
 &= 2
 \end{aligned}$$

$$\begin{aligned}
 2.7 \quad df_{\text{error}} &= (q - 1) \times (n - 1) \\
 &= (3 - 1) \times (8 - 1) \\
 &= 14
 \end{aligned}$$

$$\begin{aligned}
 2.8 \quad df_{\text{total}} &= df_{\text{between subj}} + df_{\text{intervals}} + df_{\text{error}} \\
 &= 7 + 2 + 14 \\
 &= 23
 \end{aligned}$$

$$\begin{aligned}
 2.9 \quad MS_{\text{intervals}} &= \frac{SS_{\text{intervals}}}{df_{\text{intervals}}} \\
 &= \frac{1.57}{2} \\
 &= 0.79
 \end{aligned}$$

$$\begin{aligned}
 2.10 \quad MS_{\text{error}} &= \frac{SS_{\text{error}}}{df_{\text{error}}} \\
 &= \frac{15.83}{14} \\
 &= 1.13
 \end{aligned}$$

$$\begin{aligned}
 2.11 \ F &= \frac{MS_{\text{intervals}}}{MS_{\text{error}}} \\
 &= \frac{0.79}{1.13} \\
 &= 0.69 \approx 0.70
 \end{aligned}$$

ผลย่อยของตัวแปรวัดต่างกลุ่ม

1. ผลย่อยของวิธีการปรึกษากลุ่มตามแนวทฤษฎีทางเลือกในระยะก่อนการทดลอง
(Simple effects of groups at interval = 1 “pre – test”)

$$\begin{aligned}
 1.1 \ SS_{G \text{ at Int.1}} &= \frac{79.86^2 + 75.76^2}{8} - \frac{(155.62)^2}{16} \\
 &= 1514.65 - 1513.60 \\
 &= 1.05
 \end{aligned}$$

$$\begin{aligned}
 1.2 \ SS_{w/in \text{ cells}} &= SS_{SS \text{ w/in groups}} + SS_{I \times SS \text{ w/in groups}} \\
 &= 49.25 + 44.43 \\
 &= 93.68
 \end{aligned}$$

$$\begin{aligned}
 1.3 \ MS_{w/in \text{ cells}} &= \frac{SS_{w/in \text{ cells}}}{df_{SSw/in \text{ groups}} + df_{I \times SS \text{ w/in groups}}} \\
 &= \frac{93.68}{42} \\
 &= 2.23
 \end{aligned}$$

$$\begin{aligned}
 1.4 \quad F_{G \text{ at Int.1}} &= \frac{SS_{G \text{ at Int.1}}}{MS_{w/in \text{ cells}}} \\
 &= \frac{1.05}{2.23} \\
 &= 0.47
 \end{aligned}$$

2. ผลย่อยของวิธีการปรึกษากลุ่มตามแนวทฤษฎีทางเลือกในระยะหลังการทดลอง
(Simple effects of groups at interval = 2 “post-test”)

$$\begin{aligned}
 2.1 \quad SS_{G \text{ at Int.2}} &= \frac{100.60^2 + 72.26^2}{8} - \frac{(172.86)^2}{16} \\
 &= 1917.73 - 1867.54 \\
 &= 50.19
 \end{aligned}$$

$$\begin{aligned}
 2.2 \quad F_{G \text{ at Int.2}} &= \frac{SS_{G \text{ at Int.2}}}{MS_{w/in \text{ cells}}} \\
 &= \frac{50.19}{2.23} \\
 &= 22.51
 \end{aligned}$$

3. ผลย่อยของวิธีการปรึกษากลุ่มตามแนวทฤษฎีทางเลือกในระยะติดตามผล
(Simple effects of groups at interval = 3 “Follow up”)

$$\begin{aligned}
 3.1 \quad SS_{G \text{ at Int.3}} &= \frac{99.58^2 + 77.12^2}{8} - \frac{(176.70)^2}{16} \\
 &= 1982.96 - 1951.43 \\
 &= 31.53
 \end{aligned}$$

$$\begin{aligned}
 3.2 F_{G \text{ at Int.3}} &= \frac{SS_{G \text{ at Int.3}}}{MS_{w/in \text{ cells}}} \\
 &= \frac{31.53}{2.23} \\
 &= 14.14
 \end{aligned}$$

การปรับค่า df ด้วยวิธีการของ Welch – Satterthwaite

$$f' = \frac{(u + v)^2}{\frac{u^2}{df_u} + \frac{v^2}{df_v}}$$

$$u = SS_{Ss \text{ w/in groups}} = 49.25$$

$$v = SS_{I \times SS \text{ w/in groups}} = 44.43$$

$$f' = \frac{(49.25 + 44.43)^2}{\frac{(49.25)^2}{14} + \frac{(44.43)^2}{28}}$$

$$= \frac{8775.94}{173.25 + 70.50}$$

$$= \frac{8775.94}{243.75}$$

$$= 36.00$$

$$df(g-1, f') = df(1, 36) = 4.11$$